## Bowmansgreen Primary School

## Written Calculation Progression

This document maps the progression of written formal calculation at Bowmansgreen Primary School. The progression is matched to Herts for Learning Education's ESSENTIALmaths resources and calculation policy and the formal calculation methods outlined in the National Curriculum (2013).

This progression map outlines the use of the concrete equipment, pictorial representations and abstract representations at each step of learning

The concrete, pictorial, abstract approach is a way of teaching mathematical concepts and theories in various stages, in order to help children fully understand and master what they are learning.

The concrete stage involves using items, models and objects, giving children a chance to be 'hands-on'.
The pictorial stage uses visual representations of concrete objects to model problems, encouraging children to make connections between the physical object and the picture that represents the object

The abstract stage involves using numbers and symbols to represent the method.
At the end of this document there is a glossary of the mathematical terms.

Addition

| Year group | Learning Sequence |  |
| :---: | :---: | :--- |
| 2 | 2LS15 | Step 3: Expanded written method; no regrouping (2-digit numbers) |
|  |  | Step 4: Expanded Written method; regrouping of ones (2-digit numbers) |
| 3 | 3LS8 | Step 2: Formal written method; no regrouping (3-digit numbers) |
|  |  | Step 3: Formal written method; regrouping of ones (3-digit numbers) |
|  |  | Step 4: Formal written method; regrouping of tens (3-digit numbers) |
|  |  | Step 4: Formal written method; regrouping of tens and ones (3-digit numbers) |
| 4 | 4LS4 | Step 1: Formal written method; no regrouping (4-digit numbers) * |
|  |  | Step 2: Formal written method; regrouping in hundreds, tens and ones (4-digit numbers) * |
|  |  | Step 3: Formal written method; regrouping hundreds, tens and ones causing further thousand column (4-digit numbers) * |
| 5 | 5LS10 | Step 2: Formal column addition * |

*the step is not explicitly exemplified within this progression because it is a revisit or extension of what was previously taught.

## Subtraction

| Year group | Learning Sequence |  |
| :---: | :---: | :--- |
| 2 | 2 LS17 | Step 4: Expanded written subtraction; a 2-digit number from a 2-digit number with no regrouping |
|  |  | Step 5: Expanded written subtraction; a 2-digit number from a 2-digit number with regrouping |
| 3 | 3LS9 | Step 1: Formal written subtraction; no regrouping (up to 3-digit numbers) |
|  |  | Step 2: Formal written subtraction; regrouping tens into ones (up to 3-digit numbers) |
|  |  | Step 3: Formal written subtraction; regrouping hundreds into tens (up to 3-digit numbers) |
|  |  | Step 4: Formal written subtraction; regrouping hundreds and tens (up to 3-digit numbers) |
| 4 | 4LS4 | Step 5: Formal written subtraction (revisit) * |
|  | StS10 | Step 3: Formal column subtraction * |
| 5 |  |  |

*the step is not explicitly exemplified within this progression because it is a revisit or extension of what was previously taught.

Multiplication

| Year group | Learning Sequence |  |  |  |
| :---: | :---: | :--- | :---: | :---: |
| 3 | 3LS26 | Step 3: Short multiplication; no regrouping |  |  |
|  |  | Step 4: Short multiplication; regrouping of ones into tens |  |  |
|  |  | Step 5: Short multiplication; regrouping of tens and ones |  |  |
| 4 | 4LS24 | Step 4: Short multiplication; no regrouping * |  |  |
|  |  | Step 5: Short multiplication; with regrouping causing further thousand column |  |  |
| 5 | 5LS11 | Step 1: Short multiplication; up to 3-digit numbers * |  |  |
|  |  | Step 2: Expanded vertical multiplication; 2-digit by 2-digit numbers |  |  |
|  | Step 3: Long multiplication; regrouping in first stage only, 2-digit by 2-digit numbers |  |  |  |
|  |  | Step 3: Long multiplication; regrouping in first and second stage, 2-digit by 2-digit numbers |  |  |
| 6 | 6LS12 | Step 5: Short multiplication, up to 2 decimal places by 1-digit number |  |  |
| Year 6 additional examples |  |  |  |  |
| 6 | 6LS12 | Step 3: long multiplication; 4-digit numbers by 2-digit numbers |  |  |

*the step is not explicitly exemplified within this progression because it is a revisit or extension of what was previously taught.

Division

| Year group | Learning Sequence | Step |
| :---: | :---: | :---: |
| 3 | 3LS30 | Step 2: Long division (sharing structure); sharing ones |
|  |  | Step 3: Long division (sharing structure); no regrouping (2-digit dividend) |
|  |  | Step 4: Long division (sharing structure); regrouping (2-digit dividend) |
| 4 | 4LS25 | Step 2: Long division (sharing structure); regrouping hundreds into tens (up to 3-digit numbers by 1-digit divisor) |
|  |  | Step 4: Short division (sharing structure); 1-digit divisor |
| 5 | 5LS12 | Step 2: Short division (grouping structure); regrouping tens |
|  |  | Step 3: Short division (grouping structure); regrouping hundreds and tens |
|  |  | Step 4: Short division (grouping structure); expressing quotients with fractions |
|  |  | Step 5: Short division (grouping structure); expressing quotients with decimals |
| 6 | 6LS17 | Step 2: Long division (grouping structure); up to 4-digit dividend by 2-digit divisor |
| Year 6 additional examples |  |  |
| 6 | 6LS17 | Step 4: Long division (grouping structure); up to 4-digit dividend by 2-digit divisor - expressing quotients with fractions |
|  |  | Step 5: Long division (grouping structure); up to 4-digit dividend by 2-digit divisor - expressing quotients with decimals |

*the step is not explicitly exemplified within this progression because it is a revisit or extension of what was previously taught.

## Year 2

## NC Statement:

Add and subtract numbers using concrete objects, pictorial representations, and mentally, including: - a twodigit number and ones

- a two-digit number and tens
- two, two-digit numbers

2LS15 Step 3: Expanded written method with no regrouping (2-digit numbers)

| Concrete | Pictorial |  | Abstract (Written Symbolic) |
| :---: | :---: | :---: | :---: |
| Tens Ones <br>   |  |  | 403 |
|  | $\\|\\|$ | .. | $+305$ |
| \\|l| | + \\|| |  | $\begin{array}{ll} \hline 70 & 8 \\ \hline \end{array}$ |
|  | \|||||| |  | $43+35=78$ |
| Abstract speaking frames: <br> The sum of ... ones and ... ones is ... ones. <br> The sum of ... tens and ... tens is ... tens. <br> So, $\ldots+\ldots$ is equal to ... tens and ... ones, which is ... |  |  | Notes: <br> Using embedded tens frame supports pupils to organise ones in preparation for regrouping. |

## Year 2

## NC Statement:

Add and subtract numbers using concrete objects, pictorial representations, and mentally, including: - a twodigit number and ones

- a two-digit number and tens
two, two-digit numbers
2LS15 Step 4: Expanded written method with regrouping of ones (2-digit numbers)



## Year 3

## NC Statement:

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

3LS8 Step 2: Formal written addition with no regrouping (up to three-digit numbers)


## Year 3

## NC Statement:

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

3LS8 Step 3: Formal written addition with regrouping of ones (up to three-digit numbers)


## Year 3

## NC Statement:

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

3LS8 Step 4: Formal written addition with regrouping tens only (up to three-digit numbers)


## Year 3

## NC Statement:

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

3LS8 Step 4: Formal written addition with regrouping tens and ones (up to three-digit numbers)


## Year 4

## NC Statement:

Add and subtract number with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate

4LS4 Step 3: Formal addition method with regrouping in hundreds, tens and ones causing a further thousand


## Year 5

## NC Statement:

Add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)
5LS10 step 2: Column addition


## Year 5

## NC Statement:

Add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)

5LS10 step 2: Column addition


## Year 2

## NC Statement:

add and subtract numbers using concrete objects, pictorial representations, and mentally, including: - a two digit number and ones

- a two-digit number and tens
two, two-digit numbers.
2LS17 Step 4: Expanded written subtraction, a 2-digit number from a 2-digit number with no regrouping


Pictorial


Abstract (Written Symbolic)

$$
\begin{array}{r}
80+7 \\
-\quad 30+4 \\
\hline 50+3 \\
\hline
\end{array}
$$

$$
87-34=53
$$

Notes:
Pupils should be encouraged to estimate first and
check their answer using a mental method.


## Year 3

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

3LS9 Step 1: Formal written subtraction with no regrouping (up to 3-digit numbers)


## Year 3

## NC Statement:

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

3LS9 Step 2: Formal written subtraction - regrouping tens into ones only (up to 3-digit numbers)


## Year 3

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

3LS9 Step 3: Formal written subtraction - regrouping hundreds into tens only (up to 3-digit numbers)


## Year 3

## NC Statement:

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

3LS9 Step 4: Formal written subtraction - regrouping hundreds and tens (up to 3-digit numbers)


Abstract speaking frames:
I will need to regroup..

- one hundred into ten tens. I now have ... hundreds and ... tens.
- one ten into ten ones. I now have ... tens and ... ones

Abstract (Written Symbolic)


$$
404-226=178
$$

## Notes:

Speaking frame hint: This is not a complete speaking frame. It is structured to support pupils with the language of regroup only.

## Year 4

## NC Statement:

Add and subtract number with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate

4LS4 Step 6: Formal written subtraction; regrouping of thousands


## Year 5

## NC Statement:

Add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)

5LS10 Step 3: Formal column subtraction


## Year 5

## NC Statement:

Add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)

5LS10 Step 3: Formal column subtraction


## Multiplication

## Year 3

## NC Statement:

Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods


## Year 3

## NC Statement:

Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

| 3LS26 Step 4: Short multiplication with regrouping of ones into tens only |
| :--- |
| Abstract speaking frames: <br> I. groups of ... ones is ... ones. <br> I can regroup the ... ones into ... ten(s) and ... oness). <br> ... groups of ... tens is ... tens. ... ten(s) added to ... is ... . <br> The product of ... and ... is ... . |
| Concrete |
| Notes: <br> Pupils have already met the distributive law (3LS18) <br> and rehearsed multiplying by ten (3LS25). The focus of <br> this step is to support pupils in making the connection <br> between informal distributive approach and the <br> formal layout. |
| Speaking frame note: "3 groups of 4 ones is 12 ones. I |
| can regroup the 12 ones into 1 ten and 2 ones. 3 |
| groups of 2 tens is 6 tens. 1 ten added to 6 tens is 7 |
| tens. The product of $24 \times 3$ is $72 . " ~ P u p i l s ~ s h o u l d ~ b e ~$ |
| encouraged to consider whether italicised language in |
| the speaking frame is required in the calculation. |

## Year 3

## NC Statement:

Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

3LS26 Step 5: Short multiplication with regrouping of tens and ones



Abstract speaking frames:
... groups of ... ones is ... ones.
I can regroup the ... ones into ... ten(s) and ... one(s).
... groups of ... tens is ... tens. ... ten(s) added to ... ten(s) is ..
I can regroup the ... tens into ... hundred(s) and ... ten(s)
The product of ... and ... is ... .

Notes:
At this stage, the pictorial representation is being used as a checking point to ensure pupils answer accurately. This allows focused attention on understanding the abstract recording.

Speaking frame note: " 5 groups of 7 ones is 35 ones. I can regroup the 35 ones into 3 tens and 5 ones. 5 groups of 2 tens is 10 tens. 3 tens added to 10 tens is 13 tens. I can regroup the 13 tens into 1 hundred and 3 tens. The product of $27 \times 5$ is 135 ."

## Year 4

## NC Statement:

Multiply 2-digit and 3-digit numbers by a one-digit number using formal written layout (short multiplication)

4LS24 Step 5: Formal written multiplication with regrouping which generates a new column


## Year 5

## NC Statement:

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers
5LS11 Step 2: Expanded vertical multiplication 2-digit by 2-digit


## Year 5

## NC Statement:

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

5LS11 Step 3: Long multiplication 2-digit by 2-digit with simple regrouping


## Abstract speaking frames:

First, I need to consider the ones in the multiplier.
... groups of ... ones is ones. (Do I need to regroup?)
... groups of ... tens is tens. (Do I need to regroup?)
Then, considering tens in the multiplier.
... groups of ... ones is ones. (Do I need to regroup?) ... groups of ... tens is tens. (Do I need to regroup?)
The total of all the partial products is ... .
The product of ... and ... is ... .

## Year 5

## NC Statement:

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

5LS11 Step 3: Long multiplication 2-digit by 2-digit, focusing on regroup in first partial product


## Year 5

## NC Statement:

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

5LS11 Step 3: Long multiplication 2-digit by 2-digit regrouping in first and second stage


## Year 6

## NC Statement:

Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers

6LS12 Step 5: Formal written multiplication involving numbers with up to 2 decimal places multiplied by a 1-digit number


## Year 3

## NC Statement:

Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

3LS30 Step 2: Introducing the long division method (sharing ones)

| Abstract (Written Symbolic) |
| :--- |
| Abstract speaking frames: <br> I am sharing ... ones into ... equal groups. <br> There are ... ones in each group. <br> I have ... one(s) remaining. <br> The quotient is ... with ... remainders. |
| Notes: <br> Pupils are introduced to the long division method <br> for the first time in this sequence. Short division will <br> not be introduced until pupils have understood all <br> of the stages in this expanded form. In the <br> calculation $96 \div 4$, for example, pupils often <br> struggle to understand that 1 ten will be regrouped <br> after 8 tens have been used in the 4 groups. This is <br> hidden in short division but recorded in long <br> division. |

## Year 3

## NC Statement:

Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

| 3LS30 Step 3: Long division of tens and ones with no regrouping (sharing structure) |
| :--- |
| Abstract speaking frames: <br> First, I am sharing ... tens into ... equal groups. <br> There are ... tens in each group. <br> I have ... ten(s) remaining. <br> Then, I am sharing ... ones into ... equal groups. <br> There are ... ones in each group. <br> I have ... one(s) remaining. <br> The quotient is ... with ... remainders. |
| Notes: <br> This stage is to support pupils' understanding of the <br> abstract notation. They learn to record how many <br> tens are in each group, if there are any tens <br> remaining and what the arrow means. |
| Speaking frame note: "First, I am sharing 8 tens |
| into 2 equal groups. There are 4 tens in each group. |
| I have zero tens remaining. Then, I am sharing 4 |
| ones into 2 equal groups. There are 2 ones in each |
| group. I have zero ones remaining. The quotient is |
| 42 with no remainders." |

## Year 3

Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

3LS30 Step 4: Long division of tens and ones with regrouping (sharing structure)

| Concrete | Pictorial | Abstract (Written Symbolic) |
| :---: | :---: | :---: |
|  |  | $\left.\begin{aligned} & 3 \\ & \hline 2 \\ & \hline \\ & \hline \end{aligned} \begin{array}{ll} 7 & 4 \\ \hline & 6 \end{array} \right\rvert\,$ |
|  |  | $\begin{array}{r} 1 \\ \hline \\ -\quad 1 \\ \hline \end{array}$ |
|  |  | $74 \div 2=37$ |
| Abstract speaking frames: |  | Notes: |
| First, I am sharing ... tens into ... equal groups. |  | This is a crucial stage as it demonstrates the |
| There are ... tens in each group. |  | regrouping of the remaining tens for ones and |
| I have ... ten(s) remaining. |  | how this is recorded abstractly. |
| I need to regroup the remaining ... ten(s) into ... ones. |  |  |
| I now have ... ones in total. |  | Speaking frame note: "... I have 1 ten remaining. I |
| Then, I am sharing ... ones into ... equal groups. |  | need to regroup the remaining 1 ten into 10 ones. |
| There are ... ones in each group. |  | I now have 14 ones in total..." |
| I have ... one(s) remaining. |  |  |
| The quotient is ... with ... remainders. |  |  |

## Year 4

## NC Statement:

Pupils practise to become fluent in the formal written method of short multiplication and short division with exact answers (non-statutory guidance)

4LS25 Step 2: Long division with regrouping hundreds into tens (sharing structure)


Abstract speaking frames:
First, I am sharing ... hundreds into ... equal groups.
There are ... hundreds in each group.
I have ... hundred(s) remaining.
I need to regroup the remaining ... hundreds into ...tens
I now have ... tens in total.
Next, I am sharing ... tens into .. equal groups.

$426 \div 3=142$

Notes:
Pupils revisit long division with no regrouping gin 4LS25 step 1. This is to ensure that they understand the abstract recording of long division.

Speaking frame note: This stage is an extension to the previous speaking frame - focusing on the hundreds regroup.

## Year 4

## NC Statement:

Pupils practise to become fluent in the formal written method of short multiplication and short division with exact answers (non-statutory guidance)

4LS25 Step 4: Introducing formal short division (sharing structure)

| Abstract (Written Symbolic) |
| :--- |
| Abstract speaking frames: <br> First, I am sharing ... hundreds into ... equal groups. <br> There are ... hundreds in each group. <br> I have ... hundred(s) remaining. <br> I need to regroup the remaining ... hundreds into ... tens. <br> I now have ... tens in total. <br> Next, I am sharing ... tens into .. equal groups. |
| Notes: <br> In this stage, pupils learn that the thinking <br> processes for long and short division are the same - <br> it is only the abstract written that is different. It is <br> important that pupils are able to link this to the <br> long division format and can explain the <br> compaction. |
| Speaking frame note: This stage is an extension to <br> the previous speaking frame - focusing on the <br> hundreds regroup. |

## Year 5

5LS12 Step 2: Introducing formal short division regroup from tens to ones (grouping structure)
Abstract (Written Symbolic)

| Abstract speaking frames: |
| :--- |
| How many groups of ... tens are in ... tens without regrouping? |
| I can make ... group(s) of ... tens. There is/are ... ten(s) remaining. |
| I need to regroup the ... tens into ... ones. |
| I now have ... ones. |
| How many groups of ... ones are in ... ones, without regrouping? |
| I can make ... group(s) of ... ones. |
| There is/are ... one(s) remaining. |
| There are ... groups of ... in ... with ... remainders. |


| Notes: |
| :--- |


| Pupils are encouraged to progress to a grouping |
| :--- |
| model of division. This is in preparation for 2-digit |
| divisors and understanding fractions expressed as |
| part of the quotient. Pupils should explore with |
| simple division calculations to ensure that they |
| understand the shift in structure. |

Speaking frame note: In this example, the speaking
frame would be completed like this: "How many
groups of 3 tens are in 4 tens, without regrouping?"
This is to ensure that accurate place value and
magnitude is maintained.

## Year 5

## NC Statement:

Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

| 5LS12 Step 3: Short division for numbers up to 4-digits (grouping structure) |
| :--- |
| Abstract speaking frames: <br> I want to know how many groups of ... are in ... . <br> How many groups of ... hundreds are in ... hundreds, without regrouping? <br> I can make ... group(s) of ...hundreds. <br> There is/are ... hundred(s) remaining. <br> I need to regroup the ... hundreds into ...tens. |
| Notes: <br> Speaking frame note: This is an extension <br> to the previous speaking frame. In this <br> example, the speaking frame would be <br> completed like this: "How many groups of <br> 3 hundreds are in 4 hundreds, without <br> regrouping?" This is to ensure that <br> accurate place value and magnitude is <br> maintained. |

## Year 5

## NC Statement: <br> Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

5LS12 Step 4: Short division (grouping structure) - expressing quotients with fractions


## Abstract speaking frames:

I have a remainder of ... .
This is ... (remainder) out of ... (divisor) which I need for another group.
This can be written as a fraction...
This can be simplified to... .

Abstract (Written Symbolic)
$67_{7^{115}}{ }^{\frac{1}{2}}$

$$
75 \div 6=12 \frac{1}{2}
$$

## Notes:

Speaking frame note: This is an extension to the previous speaking frame (5LS12 Step 2). In this example the speaking frame would be completed like this:
"I have a remainder of 3 .
This is 3 out of 6 which I need for another group.
This can be written as a fraction $3 / 6$.
This can be simplified to $1 / 2$."

| Year 5 | NC Statement: <br> Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context |  |
| :---: | :---: | :---: |
| 5LS12 Step 5: Short division (grouping structure) - expressing quotients with decimals |  |  |
|  | Pictorial Jottings: multiples of the divisor $\begin{gathered} 6 \\ 12 \\ 18 \\ 24 \\ 30 \\ 36 \\ 42 \\ 48 \\ 54 \\ 60 \end{gathered}$ | Abstract (Written Symbolic) $6 \longdiv { 7 ^ { 1 } 5 3 }$ $75 \div 6=12.5$ |
| Abstract speaking frames: <br> I have a remainder of ... . <br> I need to regroup the ... ones into ... tenths. <br> How many groups of ... tenths are in ... tenths, without regrouping? <br> I can make ... group(s) of ... tenths. <br> There are ... groups of ... in... . |  | Notes: <br> Speaking frame note: This is an extension to the previous speaking frame (5LS12 Step 2). In this example, the speaking frame would be completed like this: <br> "I have a remainder of 3 . <br> I need to regroup the 3 ones into 30 tenths. <br> How many groups of 6 tenths are in 30 tenths, without regrouping? <br> I can make 5 groups of 6 tenths. <br> There are 12.5 groups of 6 in $75 . "$ |

## Year 6

NC Statement:
Divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division and interpret remainders as whole number remainders fractions, or by rounding, as appropriate for the context

6LS17 Step 2: Long division for numbers up to 4 digits

|  | Pictorial Jottings: multiples of the divisor 13 26 39 52 65 78 91 104 | Abstract (Written Symbolic) $3016 \div 13=232$ |
| :---: | :---: | :---: |
| Abstract speaking frames: <br> I want to know how many groups of ... are in ... . <br> How many groups of ... thousand are in ...thousand, without regrouping? <br> I can make ... group(s) of ...thousand. <br> There is/are ... thousand(s) remaining. <br> I need to regroup the ... thousand(s) into ...hundreds. |  | Notes: <br> The structure of long division was first introduced in 3LS30, then revisited and extended in both years 4 and 5. It was revised in Step 1 of this sequence. Jottings are used to scaffold to derived related division facts. <br> Speaking frame note: This is an extension to the previous speaking frame (5LS12 Step 2). In this example, the speaking frame would be completed like this: "How many groups of 13 thousands are in 3 thousand, without regrouping?" I can make zero groups of 13 thousand. There are 3 thousand remaining. I need to regroup the 3 thousands into 30 hundreds." |

## Additional Year 6 Examples

These additional examples show only jottings, completed speaking frames and abstract recording. This complexity of calculation should only be introduced to pupils once they are confident in the conceptual pathway and can explain the abstract recording with reference to the concrete and pictorial models.
NC Statement:
Divide numbers up to 4 digits by a two-digit whole number using the formal written method
of long division and interpret remainders as whole number remainders, fractions, or by
rounding, as appropriate for the context

6LS17 Step 4: Long division for numbers up to 4 digits - expressing quotients with fractions


Abstract (Written Symbolic)
$1 5 \longdiv { 0 } \begin{array} { | l l l } { 0 } & { 3 } & { 7 } \\ { 5 } & { 6 } & { 4 } \\ { 5 } \end{array}$
$-\frac{0}{5} \quad \frac{1}{6}$
$-\begin{array}{r}4 \quad 5 \\ \hline 1\end{array}$
$-\quad \begin{array}{r}105 \\ \hline\end{array}$
$\frac{9}{15}=\frac{3}{5}$
$564 \div 15=37 \frac{3}{5}$


| $\text { Year } 6$ | NC Statement: <br> Multiply multi-digit numbers of up to 4-digits by a two-digit whole number using the formal written method of long multiplication |  |
| :---: | :---: | :---: |
| 6LS12 Step 3: Long multiplication; up to 4-digit by 2-digit |  |  |
| Abstract Speaking Frame <br> First, I need to consider the ones in the multiplier. <br> 7 groups of 6 ones is 42 ones. <br> 1 need to regroup into 4 tens and 2 ones. <br> 7 groups of 3 tens is 21 tens. <br> I need to add the regrouped 4 tens. I now have 25 tens. <br> I need to regroup into 2 hundreds and 5 tens. <br> 7 groups of 8 hundreds is 56 hundreds. <br> I need to add the regrouped 2 hundreds. I now have 58 hundreds. I can regroup this into 5 thousands and 8 hundreds. <br> Then, considering the tens in the multiplier. 20 groups of 6 ones is 120 ones. <br> I need to regroup into 1 hundred and 2 tens. 20 groups of 3 tens is 6 hundreds. <br> I need to add the regrouped 1 hundred. I now have 7 hundreds. <br> 20 groups of 8 hundred is 16 thousand. There are no regroups to add. <br> The total of the two partial products is $22,572$. The product of 836 and 27 is $22,572$. | Pictorial - jottings <br> Jottings: multiples of tricky <br> multipliers71421283542495663707784 | Abstract (Written Symbolic) $\begin{array}{r} 836 \\ \times \quad 27 \\ \hline 5852 \\ 24 \\ 16720 \\ \hline 2272 \\ \hline 2257 \end{array}$ $836 \times 27=22,572$ |

## Glossary

| Word | Definition |
| :---: | :---: |
| Regrouping | To split a number into component parts. Example: the two-digit number 38 can be partitioned into $30+8$ or $19+19$. |
| Digit | One of the symbols of a number system most commonly the symbols $0,1,2,3,4,5,6,7,8$ and 9 . Examples: the number 29 is a 2 -digit number; there are three digits in 2.95 . The position or place of a digit in a number conveys its value. |
| Equal | Symbol: =, read as 'is equal to' or 'equals' and meaning 'having the same value as'. Example: 7-2=4+1 since both expressions, $7-2$ and $4+1$ have the same value, 5 . |
| Jottings | A jotting is an informal piece of written work that is done to help work out the answer to a calculation or a problem. |
| Exchange | Change a number or expression for another of equal value. E.g. one ten for ten ones or ten ones for one ten. |
| Place value | The value of a digit that relates to its position or place in a number. Example: in 1482 the digits represent 1 thousand, 4 hundreds, 8 tens and 2 ones respectively; in 12.34 the digits represent 1 ten, 2 ones, 3 tenths and 4 hundredths respectively. |
| Distributive law | The distributive property states that multiplying a number by a group of numbers added together is the same as doing each multiplication separately. <br> For example, $5 \times(2 \times 6)=5 \times 2+5 \times 6$ |
| Remainders | In the context of division requiring a whole number answer (quotient), the amount remaining after the operation. Example: 29 divided by $7=4$ remainder 1 . |
| Fluent | To be mathematically fluent one must have a mix of conceptual understanding, procedural fluency and knowledge of facts to enable you to tackle problems appropriate to your stage of development confidently, accurately and efficiently. |
| Magnitude | The size of something. |
| Rounding | To round a number means to adjust it up or down to a number that makes calculating with it easier. Numbers are usually rounded up to the nearest 10,100 or 1000, with decimals being rounded to the nearest whole number, tenth or hundredth. There is a rule that if a digit is 4 or less it rounds down and if it is 5 or more it rounds up. |
| Multiple | A multiple is the result of multiplying one integer by another. Multiples of a number are those in that number's times table. For example, multiples of 7 include $14,35,49$ and 84 . |



| Multiplicand <br> Multiplier <br> Product | A number to be multiplied by another. e.g. in $5 \times 3,5$ is the multiplicand as it is the number to be multiplied by 3 . <br> The number you are multiplying by. <br> The result of multiplying one number by another. Example: The product of 2 and 3 is 6 since $2 \times 3=6$. multiplicand |
| :---: | :---: |
| Dividend <br> Divisor <br> Quotient | The number that is divided (the whole amount). <br> The number by which another is divided. <br> The result of a division. |
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